## General Certificate of Education (A-level) June 2012

## Mathematics

MFP2

## (Specification 6360)

Further Pure 2

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

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## Key to mark scheme abbreviations

| M | mark is for method |
| :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0 ) accuracy marks |
| -x EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

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| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 2(a) |  |  |  |  |
| (i) | Circle <br> Correct centre <br> Touching Im axis | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \end{aligned}$ | 3 | Convex loop <br> Some indication of position of centre |
| (ii) | Straight line well to left of centre | B1 |  | $\frac{1}{2} \text { line through }\left(0, \frac{1}{2}\right) \text { B0 }$ |
|  | through ( $0, \frac{1}{2}$ ) | B1 |  | Point approximately between 0 and 1 |
|  | $\perp$ to line joining ( $-2,1$ ) and ( 2,0 ) <br> NB <br> $0 / 3$ for line parallel to $x$-axis | B1 | 3 |  |
|  | $0 / 3$ for line joining the two points $(-2,1)$ and $(2,0)$ |  |  |  |
|  | $0 / 3$ for line joining $(0,0)$ to centre of circle |  |  |  |
| (b) | Minor arc indicated | B1F | 1 | ft incorrect position of line or circle |
|  | Total |  | 7 |  |

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| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a) | Use of $\cosh 2 x=2 \cosh ^{2} x-1$ | M1 |  | or $\cosh 4 x=2 \cosh ^{2} 2 x-1$ |
|  | $\text { RHS }=\frac{1}{2} \cosh 2 x+\frac{1}{2} \cosh ^{2} 2 x$ | A1 |  |  |
|  | $=\frac{1}{4}(1+2 \cosh 2 x+\cosh 4 x)$ | A1 | 3 |  |
|  | If substituted for both $\cosh 4 x$ and $\cosh 2 x$ in LHS M1 only, until corrected If RHS is put in terms of $\mathrm{e}^{x}$ M1 for correct substitution A1 for correct expansion A1 for correct result |  |  |  |
| (b) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=2 \cosh x \sinh x=\sinh 2 x$ | M1A1 |  | allow A1 for $1+\left(\frac{\mathrm{d} y}{\mathrm{~d} x}\right)^{2}=1-4 \cosh ^{2} x+4 \cosh ^{4} x$ <br> Incorrect form for $\cosh ^{2} x$ in terms of $\cosh 2 x$ M1 only |
|  | Or $\begin{aligned} & y=\left(\frac{\mathrm{e}^{x}+\mathrm{e}^{-x}}{2}\right)^{2}=\frac{\mathrm{e}^{2 x}+2+\mathrm{e}^{-2 x}}{4} \\ & \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{2 \mathrm{e}^{2 x}-2 \mathrm{e}^{x}}{4} \\ & =\sinh 2 x \end{aligned}$ | (M1) <br> (A1) |  |  |
|  | $1+\left(\frac{\mathrm{d} y}{\mathrm{~d} x}\right)^{2}=1+\sinh ^{2} 2 x=\cosh ^{2} 2 x$ | A1 | 3 | AG |
| (c) | $S=2 \pi \int_{(0)}^{(\operatorname{nn2)}} \cosh ^{2} x \cosh 2 x \mathrm{~d} x$ | M1A1 |  | allow even if limits missing |
|  | $=2 \pi \int_{0}^{\ln 2} \frac{1}{4}(1+2 \cosh 2 x+\cosh 4 x) \mathrm{d} x$ | m1 |  |  |
|  | $=\frac{2 \pi}{4}\left[x+\frac{2 \sinh 2 x}{2}+\frac{\sinh 4 x}{4}\right]$ | A1 |  | Integrated correctly |
|  | Correct use of limits $a=128, b=495$ | $\stackrel{\mathrm{m} 1}{\mathrm{~A} 1, \mathrm{~A} 1}$ | 7 | accept correct answers written down with no working. Only one A1 if $2 \pi$ not used |
|  | Total |  | 13 |  |

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